



Computer Algebra Summer Term 2019

Exercise Sheet 2. Hand in by Tuesday, April 30.

Exercise 1

Install one of the Computer algebra systems Macaulay2 or Singular on your computer.

<http://www2.macaulay2.com/Macaulay2/>

or

<https://www.singular.uni-kl.de/>

Exercise 2

Design an algorithm which for two ideal $I, J \subset P = F[x_1, \dots, x_n]$ computes

$$I : J = \{r \in P \mid rJ \subset I\}$$

Exercise 3

Let $P = F[w, x, y, z]$. Compute the syzygy module of

$$\varphi_0 : P^3 \rightarrow P^2$$

defined by

$$\varphi_0 = \begin{pmatrix} w & x & y \\ x & y & z \end{pmatrix}$$

Exercise 4

Show that

$$w^2 - xz, wx - yz, x^2 - wy, xy - z^2, y^2 - wz \in F[w, x, y, z]$$

form a GB with respect to drlex. Compute all Buchberger test syzygies among these elements and also all (second) syzygies between these test syzygies.